CALCULATION OF CHLORIN IR SPECTRUM BY DENSITY FUNCTIONAL THEORY

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The structure, frequencies of normal vibrations, and absolute intensities of bands in the IR spectra of chlorin and four of its symmetric isotopomers were calculated using DFT/B3LYP with the 6-31G(d) basis set. The force field was scaled by the Pulay method in independent and dependent natural coordinates. A method for obtaining effective force fields without using experimental data for the frequencies of fundamental vibrations was proposed. It has been demonstrated that most vibrations of the porphyrin macrocycle have characteristic frequencies upon hydrogenation of the pyrrolenine ring and only 12 vibrations differed significantly. The IR spectra of chlorin and its isotopomers were modelled. Frequencies were assigned and normal vibrations were interpreted for the examined molecules.

Key words: chorin, quantum-chemical calculation, structure, force field, dependent coordinates, linear scaling of frequency method, IR spectrum.

Most common chlorophylls of plant origin are based on the porphine structure with one hydrogenated pyrrolenine ring [1]. The presence of a saturated bond in the tetrapyrrole ring of dihyhdroporphine free base, also called chlorin, results in relaxation of the quasi-forbidden first electronic transition and the appearance of a strong absorption band in the red visible region [2]. This spectral feature that probably causes the natural selection of the basic chlorin (1) structure provides a basis for using derivatives of 1 as photosensitizers [3, 4].

An investigation of the vibrational states of **1** in the ground and excited states can reveal the vibrational frequencies of the hydrogenated pyrrolenine ring, establish correlations with the corresponding vibrations of metal complexes, and facilitate interpretation of spectra of complicated derivatives of **1**.

Frequencies found in IR spectra of 1 were first described by Mason [5]. Quasilinear absorption and fluorescence spectra of 1 incorporated into the crystal matrix of *n*-octane at 77 K were reported [6]. It has been shown that many vibrations have analogs in the spectra of porphine (2). Vibrational states of 1 and five of its isotopically substituted derivatives were investigated in detail by Raman and IR spectroscopies with theoretical analysis of normal vibrations of A_1 and B_1 symmetry types [7]. The principal results of these studies are summarized in a table that assigns frequencies for 1 [2].

Modern quantum-chemical calculations based on density-functional theory (DFT) can produce reliable data for the structure and vibrational frequencies of porphine molecules [8-10]. In this instance the vibrational equations can be solved without the limitations due to transfer of empirical force constants from molecules of related structures. It has been found [11-13] that electron correlation must be considered for a correct description of the structure and vibrational spectra of the free base **2**.

It has been noted [14-16] that the hybrid density functional method B3LYP gives the most accurate results for the structural parameters and force and electrooptical fields for multiatom molecules consisting of atoms of the first and second rows.

Our goal was to perform a quantum-chemical calculation of the force field of 1 by the B3LYP/6-31G(d) method, to assign and interpret its IR spectra [2, 7] and those of four symmetric isotopomers, to correlate completely all normal vibrations of 1 and 2, and to find the frequencies of the hydrogenated pyrrolenine fragment.

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Fig. 1 Fig. 2 Fig. 1. Structure of chlorin (1). Bond lengths (Å) and angles (deg) of porphine (2) are given in parentheses. Fig. 2. IR spectrum of chlorin (1): experimental [7] recorded in KBr disks at 300 K (1) and theoretical calculated by B3LYP/6-31G(d) (2).

Figure 1 shows the structure of **1** and the atomic numbering. The geometric parameters for the structure of **1** are not shown. Therefore, it was interesting to compare them with the corresponding values for **2** that were obtained from a single theoretical approximation. It should be noted that the hydrid functional density method with the B3LYP/6-31G(d) approximation gives accurate values for the geometric parameters for molecules consisting of atoms of the first and second periods. Uncertainties are usually less than 0.005-0.010 Å for bonds and 1-2° for angles. These are within the uncertainty limits for x-ray-structure analysis of porphines [17]. The main structural parameters of **1** and **2** given in Fig. 1 indicate that hydrogenation of one of the pyrrolenine rings at C(21) and C(22) increases the C(21)–C(22) bond length and the lengths of the two adjoining bonds C(20)–C(21) and C(22)–C(23), the values of which become characteristic of single bonds. It is also seen that hydrogenation affects the whole conjugated system. This effect is nonuniform and diminishes with distance from the reduced pyrrolenine ring. Qualitatively analogous changes are observed for the planar angles. The largest changes of ~1-4° are found for the hydrogenated pyrrolenine ring. The other angles vary in the range 0.1-1°. The NH bonds lengthen by 0.009 Å. The peripheral CH bonds are practically unchanged. The exception is the CH bond (1.096 Å) of the reduced pyrrolenine.

Hydrogenation of one of the pyrrolenine rings of **2** decreases the group symmetry from D_{2h} to C_{2v} and, as a result, more vibrations become allowed in the IR and Raman spectra.

Thus, the IR spectrum of **1** is much more complicated than that of **2**. According to selection rules, vibrations of three symmetry types, A_1 , B_1 , and B_2 , are allowed for group symmetry C_{2v} in the IR spectrum.

The molecule **1** is nonplanar. However, the porphyrin macrocycle remains planar, i.e., all its atoms lie in one plane (XY plane) (Fig. 1). The plane, in turn, is one of the symmetry planes. For sake of discussion and maintaining continuity with **2**, we separate vibrations of atoms lying in this plane into in-plane and out-of-plane ones. We analyzed normal vibrations of **1** and performed analogous calculations for four of its deuterium isomers: D(33),D(38)chlorin-d₂ (**1a**), D(27),D(30)chlorin-d₂ (**1b**), D(27),D(30),D(33),D(38)chlorin-d₄ (**1c**), and D(33),D(38),D(39),D(40)chlorin-d₄ (**1d**) (Fig. 1). Figure 2 shows experimental and calculated IR spectra of **1**.

The frequency range in which vibrations of **1** appear can be separated arbitrarily into six regions.

I. 0-90 cm⁻¹ Region. According to the calculation, only four out-of-plane vibrations of 1 are observed. Of these, two are the A_2 type and inactive in the IR spectrum; the other two are the B_2 type. One of the last two is the lowest frequency

 $v_{\text{theor}} = 39 \text{ cm}^{-1}$ vibration in **1** that is localized on the hydrogenated pyrrolenine ring and corresponds to the out-of-phase deviations of C(21) and C(22) from the plane (Fig. 1). The other three vibrations in this region are related to the out-of-plane deformation of the macrocycle as a whole.

II. 90-420 cm⁻¹ Region. Nine in-plane and seven out-of-plane vibrations lie in this region. A peculiarity of these vibrations is that the pyrrole and pyrrolenine rings vibrate as a whole. The four bands have noticeably different intensities in the experimental spectrum. Three of them with $v_{exp} = 309$, 342, and 355 cm⁻¹ are formed by in-plane vibrations; that with $v_{exp} = 321$ cm⁻¹ is out-of-plane. We note that a quantum-chemical calculation at the B3LYP/6-31G(d) level is more accurate in the low-frequency region for rigid cyclic molecules, like porphyrins. This enables the vibration at 321 cm⁻¹ to be unambiguously assigned to the B₂ type and the vibration at 309 cm⁻¹ to be reassigned to the B₁ type [2].

III. 420-680 cm⁻¹ Region. This region is characterized by the fact that only out-of-plane vibrations lie in it. According to the calculation, these have the lowest intensity. The exception is the band at 640 cm⁻¹ that corresponds to the out-of-plane (B_2) vibration and appears with a noticeable intensity in the IR spectrum.

IV. 680-900 cm⁻¹ Region. This is the most complicated region to interpret because it includes both in-plane and out-ofplane vibrations. Each band is actually a superposition of several bands. The first strong band at $v_{exp} = 705 \text{ cm}^{-1}$ is formed by five vibrations. The strongest component at $v_{theor} = 705 \text{ cm}^{-1}$ belongs to the in-plane (B₁) vibration that is due primarily to angular deformations of the pyrrole and pyrrolenine rings.

A weak band with $v_{exp} = 740 \text{ cm}^{-1}$ is formed by two in-plane vibrations of similar frequency with $v_{theor} = 735 \text{ (B}_1)$ and 738 (A₁) cm⁻¹. These are due mainly to angular deformations of the hydrogenated pyrrolenine ring and that opposite to it.

The strong band at $v_{exp} = 768 \text{ cm}^{-1}$ is formed by six vibrations, of which the strongest components, which correspond to out-of-plane vibrations at $v_{theor} = 766 (B_2)$ and $780 (B_2) \text{ cm}^{-1}$, are due to deviations of C–H bonds from the macrocycle plane. The first of these vibrations, according to the calculation, is weaker than the second and is localized on the pyrrolenine ring located opposite to the hydrogenated one. The second vibration is localized on the pyrrole rings. It should be noted that a different intensity distribution than the calculated one is observed in the experimental spectrum for these bands. The band with a maximum at $v_{exp} = 768 \text{ cm}^{-1}$ was assigned to the weaker $v_{theor} = 766 \text{ cm}^{-1}$; the shoulder on this band at $v_{exp} = 774 \text{ cm}^{-1}$, to the stronge $v_{theor} = 780 \text{ cm}^{-1}$. An analysis of the corresponding band in isotopomer **1a**, where it is resolved better owing to the difference in sensitivity of these vibrations to that type of isotopic substitution, can also confirm this assignment. The strong band with two clearly resolved maxima at $v_{exp} = 770$ and 790 cm⁻¹ corresponds to these vibrations in **1a**. According to the calculation, the relative intensity distribution on going from **1** to **1a** remains the same for these vibrations, i.e., the vibration at $v_{theor} = 787 \text{ cm}^{-1}$, to which the maximum at $v_{exp} = 790 \text{ cm}^{-1}$ corresponds in the experimental spectrum and which is much stronger than the vibration at $v_{theor} = 767 \text{ cm}^{-1}$. The situation is different in the experimental spectrum. The band at $v_{exp} = 770 \text{ cm}^{-1}$ has a wider half-width than the band with a maximum at $v_{exp} = 790 \text{ cm}^{-1}$. This is consistent with a stronger band for the former vibration.

The next strongest band with two distinct maxima at $v_{exp} = 837$ and 852 cm^{-1} is formed by two out-of-plane vibrations with $v_{theor} = 834 \text{ (B}_2)$ and $852 \text{ (B}_2) \text{ cm}^{-1}$. These are due to deviation from the C–H plane of methine bridges of the macrocycle that are adjacent to the hydrogenated ring in the first instance and symmetric to the Y axis in the second (Fig. 1). A comparison of the experimental and theoretical spectra shows that the intensity distribution for these vibrations is also inversely related to that calculated.

V. 900-1650 cm⁻¹ Region. Mainly in-plane vibrations appear in this region. The exception is a small number of outof-plane vibrations of the CH₂ group of the hydrogenated pyrrolenine ring. The bands at $v_{exp} = 944$, 958, and 1143 cm⁻¹ are most difficult to interpret. Let us examine the assignment of these bands in succession. According to the calculation, three vibrations are found in the subregion 900-970 cm⁻¹ in **1**. The first two at $v_{theor} = 954$ cm⁻¹ are accidentally doubly degenerate with the same intensity. They have symmetry types A₁ and B₁ and are due to in-plane vibrations of the pyrrolenine rings. They correspond to two close bands at $v_{exp} = 944$ and 958 cm⁻¹ in the experimental spectrum.

An analysis of the bands for the corresponding vibrations in the examined isotopomers did not provide additional information for their assignment because the frequencies of these vibrations behave almost identically and change little. It is also difficult to rely on the calculated absolute IR intensities, or more accurately on their change upon isotopic substitution in this instance, because, as shown above, the intensity distribution for certain bands in the experimental spectrum can differ from that calculated.

	1				1a		1b		1c		1d		2	
Symmetry	Ass	ignment				Calc	culated free	luencies	a a				Symmetry	Cald.
type	[2]	this work	ν	Ι	[7] v _{exp}	ν	$[7] v_{exp}$	ν	[7] v_{exp}	ν	[7] v _{exp}	ν	type	[34]
A ₁	-	-	3443	1.9	-	3443	-	3443	-	3443	-	2528	Ag	3419
A ₁	-	-	3121	0.0	-	3121	-	3121	-	3121	-	3121	Ag	3120
A ₁	-	-	3106	26.8	-	3106	-	3106	-	3106	-	3106	B_{2u}	3105
A ₁	-	-	3104	3.2	-	3104	-	3104	-	3104	-	3104	B_{2u}	3104
A ₁	-	-	3051	6.1	-	3051	-	2252	-	2252	-	3051	Ag	3054
A ₁	-	-	3045	14.3	-	2248	-	3045	-	2248	-	2248	B ₂₁₁	3054
A ₁	-	-	2926	41.3	-	2926	-	2926	-	2926	-	2926	Ag	3106
A ₁	1623	1623	1624	294.7	1611	1615	1620	1624	1610	1615	1600	1608	B ₂₁₁	1594
A_1	_	1600	1602	24.8	1595	1602	1587	1591	1583	1591	_	1598	Ag	1602
A ₁	-	-	1548	4.2	_	1547	_	1545	_	1543	-	1546	Ag	1555
A_1	1524	1524	1535	32.1	1517	1531	1517	1534	1513	1530	1510	1526	B ₂ .,	1543
A ₁	-	1467	1491	35.3	1467	1491	1464	1486	1463	1486	1460	1484	B2.	1494
A ₁	-	_	1481	0.2	_	1481	_	1481	_	1480	_	1479	Ag	1504
A_1	1443	1432	1452	3.6	1414	1434	1433	1452	1416	1432	1415	1434	Ag	1433
A_1	1418	1418	1419	1.3	1371	1379	1416	1414	1383	1379	1366	1370	B ₂ ,	1411
A_1	-	-	1399	7.9	_	1402	-	1359	_	1356	_	1394	Ag	1402
A_1	-	-	1364	0.2	-	1364	-	1367	-	1367	-	1360	B ₂ ,	1354
A_1	-	1337	1350	1.4	1325	1338	1326	1328	1304	1314	1322	1330	Ag	1351
A_1	1354	_	1256	5.2	1248	1249	-	1235	1206	1215	1092	1093	B ₂ ,	1248
A_1	1256	1256	1243	26.6	_	1230	1247	1245	1246	1245	1249	1248	B_{2u}	1238
A_1	1219	1219	1224	27.9	1210	1221	1223	1224	1206	1222	1218	1227	Ag	1061
A_1	1171	1171	1174	49.1	_	940	914	924	_	940	_	934	Ag	1179
A_1	-	-	1158	4.1	1160	1165	1166	1166	923	924	1163	1168	B ₂ ,	1159
A_1	1060	1060	1064	0.9	-	1064	1061	1062	1066	1062	_	1063	Ag	1067
A_1	-	1052	1054	28.4	1052	1055	1061	1066	1066	1068	1051	1054	B ₂ ,	1058
A ₁	981	-	998	0.0	1014	1011	-	997	1016	1014	985	1003	Ag	1504
A_1	964	981	984	13.8	987	985	996	1006	999	1001	-	864	Ag	987
A_1	_	_	975	4.1	_	977	_	975	_	976	-	974	B ₂ .,	987
A_1	-	958	954	33.1	955	954	954	958	960	958	957	956	Ag	951
A ₁	797	_	860	0.5	_	853	_	860	854?	853	-	853	B2.,	947
A ₁	784	-	772	0.5	-	767	-	766	-	759	730	735	B_{2u}	772
A ₁	_	740	738	14.6	730	731	-	729	692	653	712	729	B2.	740
A_1	720	720	718	5.2	-	677	-	672	660	660	-	676	Ag	721
A ₁	705	-	712	0.7	-	700	-	701	692	692	-	700	Ag	716
A_1	355	355	349	7.7	356	348	350	348	350	347	-	348	B2.,	350
A_1	309	-	299	0.0	_	299	-	299	_	298	-	297	Ag	304
A_1	-	-	286	0.0	-	284	-	284	-	283	-	276	B ₂₁	287
\mathbf{B}_{1}	-	-	151	0.2	-	151	-	151	-	151	-	151	Ag	153
B ₁	-	-	3407	64.1	-	3407	-	3407	-	3407	-	2505	B3.,	3381
B ₁	-	-	3121	20.8	-	3121	-	3121	-	3121	-	3121	B ₃ ,	3119
B ₁	-	-	3104	0.1	-	3104	-	3104	-	3104	-	3104	Big	3104
B ₁	-	-	3085	4.7	-	3085	-	3085	-	3085	-	3085	Big	3086
\mathbf{B}_{1}	-	-	3051	9.6	-	3051	-	2252	-	2252	-	3051	B ₃₁₁	3054
B ₁	-	-	3045	10.3	-	2247	-	3045	-	2247	-	2247	Big	3054
B ₁	-	-	2917	14.7	-	2917	-	2917	-	2917	-	2917	B3.	3086
B ₁	1600	1600	1600	30.9	1595	1597	1594	1594	1583	1590	-	1588	$B_{1\sigma}$	1590
\mathbf{B}_{1}	1600	1524	1534	40.5	1517	1530	1517	1530	1513	1527	1519	1528	B3,,	1509
B ₁	1510	1510	1523	3.2	-	1513	-	1516	-	1503	-	1510	B _{3u}	1522

TABLE 1. Interpretation of Experimental Vibrational IR Spectrum [2, 7] of Chlorin (1) and Correlation with Porphine (2) Vibrations. Absolute Intensities of IR Absorptions (I), qm/mol; Frequencies (v), cm⁻¹

TABLE 1. (continued)

	1				1a		1b		1c		1d		2	
Symmetry	Assignment				Calc	ulated frequencies		1				Symmetry	Cald.	
type	[2]	this work	ν	Ι	[7] v _{exp}	ν	[7] v _{exp}	ν	[7] v _{exp}	ν	[7] v _{exp}	ν	type	[34]
B_1	-	-	1488	1.4	-	1473	-	1482	-	1469	-	1466	B _{lg}	1493
B_1	1467	1443	1457	1.3	1437	1456	1442	1456	1438	1456	1437	1456	-	-
B_1	1432	1400	1406	60.8	-	1375	1398	1390	1361	1363	1378	1373	B_{3u}	1403
B_1	1400	-	1395	0.1	1395	1398	1398	1399	1383	1390	1389	1393	B_{3u}	1406
B_1	-	-	1377	0.1	1371	1378	-	1375	1383	1377	-	1376	B _{lg}	1381
B_1	-	1354	1358	9.2	1332	1346	-	1322	-	1316	1322	1339	B_{lg}	1357
B_1	1306?	1306	1310	22.9	1305	1308	1305	1306	1304	1306	1303	1308	B _{lg}	1319
B_1	1337	1270	1276	1.4	-	1271	-	1265	1246	1253	-	1269	B_{3u}	1286
B_1	1270	1233	1238	2.5	1210	1223	1211	1224	-	1217	-	1092	B _{lg}	1233
B_1	1233	-	1187	0.8	1179	1180	-	1181	1172	1171	-	1190	B _{lg}	1191
B_1	-	1171	1172	13.1	924	924	-	1170	923	924	921	922	B_{3u}	1143
B_1	-	1143	1169	63.4	1142	1170	1140	1165	1140	1166	1142	1167	B_{3u}	1199
B_1	-	-	1141	1.9	-	1141	914	917	914	916	-	1148	B _{lg}	1140
B_1	1052	1037	1045	110.2	1036	1046	1039	1046	1042	1048	1037	1046	B _{3u}	1053
B_1	1000	1000	1002	5.0	-	1002	996	999	999	999	985	1001	B_{3u}	997
B_1	958	-	975	3.3	-	978	975	979	-	980	-	858	B _{lg}	976
B_1	958	964	962	94.7	963	963	969	968	970	972	957	956	B_{3u}	969
B_1	944	944	954	33.9	945	952	947	954	948	952	944	951	B _{lg}	1002
B_1	797	784	792	13.3	-	791	-	782	-	781	785	786	B _{lg}	797
B_1	784	-	776	4.5	-	770	-	769	-	757	-	721	B _{lg}	777
B_1	740	740	735	9.7	-	726	-	724	-	719	720	731	B_{3u}	775
B_1	705	705	705	51.1	694	684	694	689	-	671	678	683	B_{3u}	722
B_1	-	-	402	0.0	-	402	-	402	-	402	-	402	B _{lg}	410
B_1	-	-	387	0.1	-	384	-	384	-	380	-	377	B _{lg}	387
B_1	342	342	335	10.1	340	335	340	335	338	334	-	334	B_{3u}	350
B_1	-	309	307	2.4	305	305	300	305	-	303	-	304	B_{3u}	309
B_1	-	-	96	0.0	-	95	-	95	-	95	-	94	B _{lg}	100
B_2	-	-	2961	28.4	-	2961	-	2961	-	2961	-	2961	-	-
B_2	1143?	-	1130	0.0	-	1130	-	1130	-	1130	-	1130	-	-
B_2	1037?	(897)	886	3.1	903	885	-	882	-	881	880	885	B _{3g}	890
B_2	852	852	852	92.8	855	850	-	622	622	622	855	850	B _{lu}	850
B_2	837	837	834	20.6	618	616	837	836	622	616	620	616	B _{3g}	838
B_2	774	797	807	15.8	-	818	-	808	-	818	-	818	-	-
B_2	768	768	780	133.5	790	787	785	787	790	794	785	778	B_{lu}	792
B_2	716	774	766	31.7	770	767	-	773	-	775	771	761	B _{3g}	768
B_2	694	716	724	21.1	730	733	-	736	740	742	504	525	B _{lu}	732
B_2	-	694	693	7.8	714	694	-	703	714	709	692	691	B _{3g}	697
B_2	-	-	680	0.0	-	690	-	682	-	690	-	697	B_{lu}	639
B_2	-	(640)	640	1.0	640	641	650	651	660	653	-	644	B _{lu}	639
B_2	-	-	572	0.5	565	568	-	572	582?	568	570	578	B _{3g}	663
B_2	-	-	422	0.5	-	418	412	409	-	402	-	418	B_{3g}	433
B ₂	-	(321)	314	3.6	305	300	300	300	-	287	-	300	B _{lu}	329
B ₂	-	-	208	0.5	-	207	-	206	-	206	-	206	B _{lu}	205
B ₂	-	-	198	0.9	-	195	-	198	-	194	-	195	B_{3g}	203
B ₂	-	-	130	0.1	-	129	-	129	-	128	-	129	B_{3g}	131
B ₂	-	-	97	7.1	-	97	-	97	-	97	-	96	B _{lu}	93
B_2	-	-	51	0.2	-	51	-	51	-	51	-	51	B _{lu}	55

^aFrequencies obtained from force-field scaling; reassigned frequencies appear in bold; new assignments are given in parentheses; assumed assignments² are marked with ?.

1 ^a	1a	1b	1c	1d	2	
	Calculated vi	Symmetry type	Cald. [18]			
2943	2943	2943	2943	2943	-	-
1222	1222	1222	1222	1222	-	-
1005	1004	1005	1004	1004	$B_{l\sigma}$	1002
887	887	882	881	887	Au	892
874	874	872	871	874	Au	880
839	838	730	599	838	$B_{2\sigma}$	839
817	620	820	620	615	Au	828
766	777	773	785	775	B_{2g}	772
687	687	601	732	687	$B_{2\sigma}^{-g}$	696
683	700	683	700	698	Au	1238
660	660	661	662	651	$B_{2\sigma}$	671
611	606	613	611	459	B_{2g}^{-g}	627
540	515	540	514	517	Au	470
449	449	432	432	445	B_{2g}	420
326	323	325	322	323	Au	293
203	199	201	196	199	B_{2g}	184
126	126	126	126	122	B_{2g}	125
84	83	82	81	83	Au	66
38	38	38	38	38	Au	694

TABLE 2. Calculated Vibrational Frequencies (v, cm⁻¹) for Chlorin (1) and Isotopomers (1a, 1b, 1c, 1d) of Chlorin and Porphine (2) That are IR Inactive

Symmetry type of 1: A_2 ; ^afrequencies obtained from force-field scaling.

Considering that one of the bands is formed by the totally symmetric vibration, we used experimental data obtained from the fluorescence spectrum [18] recorded in an *n*-octane matrix at 5 K to assign it more reliably. A strong band at $v_{exp} = 956 \text{ cm}^{-1}$ is observed in the fluorescence spectrum of **1**. The band closest in frequency in the IR spectrum is that at $v_{exp} = 958 \text{ cm}^{-1}$, which we assigned to the fully symmetric vibration. The third band in this subregion at $v_{exp} = 964 \text{ cm}^{-1}$ was assigned to the in-plane B₁ vibration at $v_{theor} = 962 \text{ cm}^{-1}$, which is due primarily to a vibration of the pyrrole rings.

According to the calculation, seven principal vibrations that are active in the IR spectrum are found in the 1100-1200 cm⁻¹ subregion for **1**. Two of these at $v_{\text{theor}} = 1169$ and 1174 cm^{-1} are very strong. They are similar in frequency and form only one strong band in the theoretical spectrum. On the other hand, two well resolved bands at $v_{\text{exp}} = 1143$ (middle) and 1171 cm⁻¹ (strong) are observed in the experimental spectrum.

An interesting feature of the first band is its insensitivity [2, 7] to isotope substitution in the *meso*-positions and the macrocycle center. Based on this [2, 7], it has been assumed that this band is a twisting vibration of the CH₂ group of the hydrogenated pyrrolenine ring. According to the calculation, the frequency of this vibration is 1130 cm⁻¹ and it is very weak. On the other hand, this subregion contains an in-plane vibration at $v_{\text{theor}} = 1169 \text{ cm}^{-1}$ of symmetry type B₁ that is also insensitive to the examined types of deuteration. A peculiarity of the shape of this vibration is the simultaneous shift of all N atoms in one direction (along the x axis). Despite the significant difference between the calculated and experimental frequencies (26 cm⁻¹), the band at $v_{exp} = 1143 \text{ cm}^{-1}$ was assigned to just this vibration. The correctness of this assignment was confirmed based on a comparison of the vibrations of 1 and 2, the IR spectrum of which was interpreted in detail [19-23]. The examined vibration in 2 corresponds to one analogous in shape and practically insensitive to deuteration at $v_{exp} = 1177 \text{ cm}^{-1}$. Its calculated value, like for 1, is increased by 28 cm⁻¹.

The subregion 1500-1610 cm⁻¹ in the IR spectrum of **1** contains two relatively broad bands at $v_{exp} = 1524$ and 1590 cm⁻¹. According to the calculation, these are formed by two pairs of in-plane vibrations at $v_{theor} = 1534$ (B₂) and 1535 (A₁) cm⁻¹ and $v_{theor} = 1600$ (B₁) and 1602 (A₁) cm⁻¹ that are similar in frequency and strength. In such instances, Table 1 contains a single experimental value for each pair of vibrations.



Fig. 3. Change of bond force constants (in units of 10^6 cm⁻²) for **1** compared with **2**. Thick, thin, and normal lines are bonds for which the force constants are increased, decreased, and unchanged, respectively.

The assignments of the frequencies and the interpretation of the other bands causes no serious difficulties and are listed in Table 1 together with the analogous values for isotopomers **1a**, **1b**, **1c**, and **1d**. Table 2 lists the calculated frequencies of the vibrations of A_2 symmetry that are inactive in the IR spectra.

Deriving force constants (FC) in dependent natural coordinates enables them to be compared correctly by analysis in homologous series. We analyzed in detail FC of **1** and **2** produced in a single basis of dependent natural coordinates.

The change of bond FC on going from 2 to 1 is nonlocal in nature (Fig. 3). Such behavior of the FC is due to a change in the nature of the conjugation in 1. The greatest changes, as expected, occur for FC of bonds and angles of the hydrogenated fragment. Thus, FC of the C(20)–C(21) bond decrease by ~15%; of the C(21)–C(22) bond, by ~43%. The FC of the C(20)–N(4) bond of the hydrogenated fragment increases by ~3%; of the C(20)–C(19) bond, which adjoins the methine bridge, by ~5%. All FC of the internal angles of the hydrogenated fragment and adjoining angles C(19)–C(20)–C(21) and C(19)–C(20)–N(4) decrease. FC of bonds and angles not adjoining the hydrogenated fragment decrease differently. A slight qualitative trend in the change of FC of conjugated bonds can be seen as an alternation of their signs along the chain that begins at methine bridge C(19)–C(20) and passes through the pyrrole CN bond and CC bond of the pyrrolenine ring, terminating at the C(11)–C(12) bond. This correlation between the changes of FC for bonds and those of the corresponding lengths showed that they are in complete qualitative agreement, i.e., the signs of the changes coincide in all instances.

Furthermore, comparison of **1** and **2** shows that several off-diagonal elements of the force field that define the interaction undergo relatively large changes. The most significant changes occur for elements of the close and distant interactions of coordinates for the hydrogenated fragment. The magnitude of the interaction element between the C(21)–C(22) bond, which becomes single in **1**, and the C(20)–N(4) bond of the same ring decreases by 25%. The interaction of this bond with the C(20)–N(4)–C(23) bond also decreases by half. The size of the interaction between the CN bonds of the hydrogenated ring changes by an order of magnitude. The interaction element changes sign. The size of distant interaction between the C(21)–C(22) and C(8)–N(1) bonds decreases by five times. The interaction between C(21)–C(22) and C(7)–C(8) decreases almost to zero. The overall statistics for the change of FC of the porphyrin macrocycle upon hydrogenation of one pyrrolenine ring indicates that ~30% of the FC change in absolute magnitude by more than 0.001×10^6 cm⁻² and ~1% of off-diagonal elements change by more than 0.1×10^6 cm⁻².

Thus, a comparison of the FC leads to the same conclusion as an analysis of the structural changes: A local change of the conjugation chain in one of its parts not only causes local changes in the adjacent parts but also overall changes in the parameters of the whole chain.

The nature of the change of FC upon this type of substitution indicates that the FC of 2 cannot be used to predict the vibrations of 1 by taking into account only introduction of local adjustments for the substituent as, for example, was done successfully for substituted benzenes [24], where the nature of the ring conjugation did not change upon substitution. The Pulay method of transferring scaling factors or its combination with linear frequency scaling do not have these drawbacks.

In addition to the comparison of the FC, the vibrational states of **1** should be compared with their analogs in **2**, which are structurally more symmetric, for a deeper understanding. Vibrations for a homologous series of compounds must also be completely correlated in order to assign them using frequency shifts [25]. The similarity of frequencies for certain vibrations of **2** and **1** was first noted during an investigation of fine-structure absorption and fluorescence spectra [6]. All frequencies of **2** were correlated by us with the corresponding frequencies of **1** on the basis of an analysis using natural coordinates and a detailed comparison of Descartes shifts of atoms during vibrations (Tables 1 and 2). The correctness of the correlations was monitored using correlations of symmetry types on going from $D_{2h}(2)$ to $C_{2v}(1)$: $A_g, B_{2u} \rightarrow A_g$; $B_{1g}, B_{3u} \rightarrow B_1$; $A_u, B_{2g} \rightarrow A_2$; $B_{3g}, B_{2g} \rightarrow B_2$. As it turned out, the shapes and frequencies of 99 vibrations of **1** are changed little compared with those of **2** and only 15 change significantly. An absolute frequency change exceeding 20 cm⁻¹ was arbitrarily considered significant. The sharp decrease of FC for the C(20)–C(21), C(21)–C(22), and C(22)–C(23) bonds is explained by the appearance of strongly localized vibrations of the hydrogenated pyrrolenine ring at 863, 955, and 1000 cm⁻¹. The specifics for **1** are the rocking (809, 1006 cm⁻¹), twisting (1131, 1222 cm⁻¹), wagging (1225, 1275 cm⁻¹), and scissoring (1453, 1478 cm⁻¹) vibrations of the CH₂ group. Six of these are active in the IR spectrum. Only two of medium strength are observed experimentally.

Thus, the structure and IR spectra of **1** and four of its isotopomers of group C_{2v} are calculated using the B3LYP/6-31G(d) method. A new assignment for 20 vibrational bands that are observed experimentally in the IR spectrum of **1** is proposed. Vibrations between **1** and four of its symmetric isotopomers are correlated. Taking into account this correlation, a full interpretation of the vibrational IR spectra of the examined isotopomers is given.

A method for obtaining effective FC of complex molecules is proposed that is based on combined use of the linear frequency scaling method and the Pulay method of scaling quantum-mechanical force fields that is used to obtain force fields for **1** and **2** in dependent natural coordinates.

The Descartes shifts for vibrations and potential-energy distributions were compared in order to assign fully the normal vibrations of **1** and **2**. Vibrations of the hydrogenated fragment in **1** were found.

EXPERIMENTAL

Structures, frequencies of normal vibrations, and absolute band intensities in the IR spectra of **1** were calculated by quantum mechanics using programs [26] with the B3LYP/6-31G(d) hybrid three-parameter functional density approximation. Vibrations of **1** were described using the same types of natural coordinates as for **2** [19-22] and tetraazaporphine [25, 28], which were investigated previously. The full basis set consisted of 144 natural coordinates. The molecule **1** belongs to point group C_{2v} . Its vibrations are distributed by symmetry types as follows: $38A_1 + 37B_1 + 19A_2 + 20B_2$. The quantum-mechanical force field was scaled in dependent [28] and independent natural coordinates using the Pulay method [29-31] and a published algorithm [32].

The quantum-mechanical force field was refined using frequencies calculated using a linear scaling method [23, 33, 34] and the equation

$$v_{exp}/v_{theor} = av_{theor} + b$$
,

where v_{exp} and v_{theor} are the experimental and calculated frequencies in cm⁻¹ and $a = -8.35(3) \times 10^{-6}$ and b = 0.9813(4) are empirical constants obtained [23] for the 6-31G(d) basis set.

Frequencies were scaled linearly using literature data [23, 25, 27] to predict the experimental frequencies of **2** and tetraazaporphine. The average absolute deviation of the calculated frequencies from the experimental ones for **2** was 6.2 cm⁻¹; for tetraazaporphine, 5.9 cm⁻¹. For comparison, these same values for the force field refined using experimental frequencies were 5.7 and 5.8 cm⁻¹, respectively. The described method was used to obtain the effective force field of ethylchlorophyllide *a* and to interpret the vibrational IR spectrum of chlorophyll *a* [35].

Force fields of 1 and 2 were compared in dependent natural coordinates. IR spectra of 1 and its isotopomers were modelled by resolving shapes of individual bands. The shape was described by a Lorentzian function normalized over the integrated band strength. The half-widths of all bands was 5 cm⁻¹.

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